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**Edexcel**

## **Mark Scheme (Results)**

**Summer 2018**

**Pearson Edexcel GCE Further Mathematics  
Statistics S3 Paper 6691\_01**

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

# EDEXCEL GCE MATHEMATICS

## General Instructions for Marking

1. The total number of marks for the paper is 75.
2. The Edexcel Mathematics mark schemes use the following types of marks:
  - M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
  - A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
  - B marks are unconditional accuracy marks (independent of M marks)
  - Marks should not be subdivided.
3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod – benefit of doubt
  - ft – follow through
  - the symbol  $\surd$  will be used for correct ft
  - cao – correct answer only
  - cso - correct solution only. There must be no errors in this part of the question to obtain this mark
  - isw – ignore subsequent working
  - awrt – answers which round to
  - SC: special case
  - oe – or equivalent (and appropriate)
  - dep – dependent
  - indep – independent
  - dp decimal places
  - sf significant figures
  - \* The answer is printed on the paper
  - $\square$  The second mark is dependent on gaining the first mark
4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
  5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
  6. If a candidate makes more than one attempt at any question:
    - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
    - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
  7. Ignore wrong working or incorrect statements following a correct answer

| Question Number | Scheme  | Marks                   |   |   |    |    |   |    |    |   |  |   |   |   |   |   |   |   |   |   |  |   |   |   |   |   |   |   |   |   |  |   |    |   |   |   |    |    |   |    |  |       |   |   |   |   |   |   |   |   |    |                           |
|-----------------|---|-------------------------|---|---|----|----|---|----|----|---|--|---|---|---|---|---|---|---|---|---|--|---|---|---|---|---|---|---|---|---|--|---|----|---|---|---|----|----|---|----|--|-------|---|---|---|---|---|---|---|---|----|---------------------------|
| 1. (a)          | $r = \frac{S_{ca}}{\sqrt{S_{cc}S_{aa}}} = \frac{47.7625}{\sqrt{34787.5 \times 0.217287}} = 0.549361\dots$   | B1<br>(1)               |   |   |    |    |   |    |    |   |  |   |   |   |   |   |   |   |   |   |  |   |   |   |   |   |   |   |   |   |  |   |    |   |   |   |    |    |   |    |  |       |   |   |   |   |   |   |   |   |    |                           |
| (b)             | $H_0 : \rho = 0, H_1 : \rho > 0$<br>(0.549 <) 0.6215 (Not significant Insufficient evidence to reject $H_0$ )<br>Insufficient evidence of a positive correlation between the <b>concentration of a radioactive element</b> and the <b>amount of dissolved solids</b> in groundwater.  | B1<br>B1<br>B1ft<br>(3) |   |   |    |    |   |    |    |   |  |   |   |   |   |   |   |   |   |   |  |   |   |   |   |   |   |   |   |   |  |   |    |   |   |   |    |    |   |    |  |       |   |   |   |   |   |   |   |   |    |                           |
| (c)             | <table border="1"> <thead> <tr> <th>Sample</th> <th>A</th> <th>B</th> <th>C</th> <th>D</th> <th>E</th> <th>F</th> <th>G</th> <th>H</th> <th></th> </tr> </thead> <tbody> <tr> <td>c</td> <td>2</td> <td>6</td> <td>4</td> <td>3</td> <td>7</td> <td>1</td> <td>8</td> <td>5</td> <td></td> </tr> <tr> <td>a</td> <td>4</td> <td>5</td> <td>1</td> <td>3</td> <td>8</td> <td>2</td> <td>6</td> <td>7</td> <td></td> </tr> <tr> <td>d</td> <td>-2</td> <td>1</td> <td>3</td> <td>0</td> <td>-1</td> <td>-1</td> <td>2</td> <td>-2</td> <td></td> </tr> <tr> <td><math>d^2</math></td> <td>4</td> <td>1</td> <td>9</td> <td>0</td> <td>1</td> <td>1</td> <td>4</td> <td>4</td> <td>24</td> </tr> </tbody> </table> <p>Note Reverse ranks <math>\sum d^2 = 144</math></p> $r_s = 1 - \frac{6\sum d^2}{n(n^2 - 1)} = 1 - \frac{6 \times 24}{8(64 - 1)} = 0.71428\dots$ | Sample                  | A | B | C  | D  | E | F  | G  | H |  | c | 2 | 6 | 4 | 3 | 7 | 1 | 8 | 5 |  | a | 4 | 5 | 1 | 3 | 8 | 2 | 6 | 7 |  | d | -2 | 1 | 3 | 0 | -1 | -1 | 2 | -2 |  | $d^2$ | 4 | 1 | 9 | 0 | 1 | 1 | 4 | 4 | 24 | M1<br>M1A1<br>M1A1<br>(5) |
| Sample          | A   | B                       | C | D | E  | F  | G | H  |    |   |  |   |   |   |   |   |   |   |   |   |  |   |   |   |   |   |   |   |   |   |  |   |    |   |   |   |    |    |   |    |  |       |   |   |   |   |   |   |   |   |    |                           |
| c               | 2   | 6                       | 4 | 3 | 7  | 1  | 8 | 5  |    |   |  |   |   |   |   |   |   |   |   |   |  |   |   |   |   |   |   |   |   |   |  |   |    |   |   |   |    |    |   |    |  |       |   |   |   |   |   |   |   |   |    |                           |
| a               | 4   | 5                       | 1 | 3 | 8  | 2  | 6 | 7  |    |   |  |   |   |   |   |   |   |   |   |   |  |   |   |   |   |   |   |   |   |   |  |   |    |   |   |   |    |    |   |    |  |       |   |   |   |   |   |   |   |   |    |                           |
| d               | -2  | 1                       | 3 | 0 | -1 | -1 | 2 | -2 |    |   |  |   |   |   |   |   |   |   |   |   |  |   |   |   |   |   |   |   |   |   |  |   |    |   |   |   |    |    |   |    |  |       |   |   |   |   |   |   |   |   |    |                           |
| $d^2$           | 4   | 1                       | 9 | 0 | 1  | 1  | 4 | 4  | 24 |   |  |   |   |   |   |   |   |   |   |   |  |   |   |   |   |   |   |   |   |   |  |   |    |   |   |   |    |    |   |    |  |       |   |   |   |   |   |   |   |   |    |                           |
| (d)             | $H_0 : \rho_s = 0, H_1 : \rho_s > 0$<br>(0.714 >) 0.6429 (Significant. Reject $H_0$ )<br>Evidence of a positive correlation between the <b>concentration of a radioactive element</b> and the <b>amount of dissolved solids</b> in groundwater.   | B1<br>B1<br>B1ft<br>(3) |   |   |    |    |   |    |    |   |  |   |   |   |   |   |   |   |   |   |  |   |   |   |   |   |   |   |   |   |  |   |    |   |   |   |    |    |   |    |  |       |   |   |   |   |   |   |   |   |    |                           |
| (e)             | Results of tests suggest (monotonic) <b>non-linear</b> relationship or assumptions for PMCC breached i.e. <b>not</b> (joint) <b>normal</b> .  | B1<br>(1)               |   |   |    |    |   |    |    |   |  |   |   |   |   |   |   |   |   |   |  |   |   |   |   |   |   |   |   |   |  |   |    |   |   |   |    |    |   |    |  |       |   |   |   |   |   |   |   |   |    |                           |
| <b>Total 13</b> |   |                         |   |   |    |    |   |    |    |   |  |   |   |   |   |   |   |   |   |   |  |   |   |   |   |   |   |   |   |   |  |   |    |   |   |   |    |    |   |    |  |       |   |   |   |   |   |   |   |   |    |                           |

### Notes

|     |  |
|-----|--|
| (a) | 1 <sup>st</sup> B1 awrt 0.549  |
| (b) | 1 <sup>st</sup> B1 Both correct. Require population parameter $\rho$ and one tailed test.<br>2 <sup>nd</sup> B1 cv 0.6215<br>3 <sup>rd</sup> B1 Context required. Must mention <b>concentration of a radioactive element</b> and <b>amount of dissolved solids</b>   |
| (c) | 1 <sup>st</sup> M1 for an attempt to rank the concentration of a radioactive element <b>and</b> the amount of dissolved solids with at least 4 correct for each variable. Allow reverse ranks.<br>2 <sup>nd</sup> M1 for attempt at $d^2$ row<br>1 <sup>st</sup> A1 all correct<br>3 <sup>rd</sup> M1 for use of the correct formula and an attempt to rank, follow through their $\sum d^2$ if clearly stated<br>If answer is not correct, a correct expression is required.<br>A1 awrt 0.714               |
| (d) | 1 <sup>st</sup> B1 for both hypotheses in terms of $\rho$ , one tail $H_1$ . Allow use of $\rho_s$ .<br>Alternative hypothesis compatible with their ranking.<br>2 <sup>nd</sup> B1 for cv of 0.6429<br>3 <sup>rd</sup> B1ft for a correct contextualised comment. Must mention <b>concentration of a radioactive element</b> and the <b>amount of dissolved solids</b> . Follow through their $r_s$ and their cv (provided it is $ cv  < 1$ )<br>Don't insist on the word "positive" for a one-tailed test. |
| (e) | B1 for ' <b>non-linear</b> ' oe, or ' <b>not normal</b> '  |

| Question Number                     | Scheme  | Marks  |
|-------------------------------------|---|--|
| <p>2. (a)</p> <p>(b)</p> <p>(c)</p> | <p><b>Record / List</b> all ticket numbers of <b>standard</b> and <b>premium</b> tickets<br/>Use <b>random numbers</b> to select a sample of standard and a sample of premium ticket holders i.e. <b>within strata</b>.<br/><b>Sample sizes in proportion</b> to the no of standard and no of premium ticket holders at the concert.</p> <p><math>H_0 : \mu_p - \mu_s = 6</math> oe [ <math>p = \text{premium } s = \text{standard}</math> ]<br/><math>H_1 : \mu_p - \mu_s &gt; 6</math> oe</p> <p>Standard error = <math>\sqrt{\frac{10^2}{60} + \frac{8^2}{55}} = [\sqrt{2.83030\dots}] = [1.682\dots]</math></p> <p><math>z = \frac{\pm(23 - 15 - 6)}{\sqrt{\frac{10^2}{60} + \frac{8^2}{55}}}</math><br/>= <math>\pm 1.1888\dots</math> awrt <math>\pm 1.19</math></p> <p>cv 5% one tailed = 1.6449<br/>Not significant, insufficient evidence to reject <math>H_0</math><br/>Insufficient evidence to support the <b>manager's claim</b><br/><u>or</u> the mean value of merchandise sold to premium ticket holders is NOT more than £6 greater than the mean value of merchandise sold to standard ticket holders.</p> <p><b>Sample size is large</b> so <b>Central Limit Theorem (CLT)</b> applies so <b>do not need to assume merchandise sold</b> has a normal distribution.</p>   | <p>B1<br/>B1<br/>B1<br/>(3)</p> <p>B1<br/>B1<br/>M1<br/>dM1<br/>A1<br/>B1<br/>dM1<br/>A1cso<br/>(8)</p> <p>B1<br/>dB1<br/>(2)</p> <p><b>Total 13</b></p> |
| <b>Notes</b>                        |   |  |
| <p>(a)</p> <p>(b)</p> <p>(c)</p>    | <p>1<sup>st</sup> B1 Sampling frame in context. Accept list of all standard and premium ticket holders at the concert.<br/>2<sup>nd</sup> B1 Use of <b>random selection</b> eg simple random sampling <b>within strata</b><br/>3<sup>rd</sup> B1 Accept description of <math>n_s, n_p</math>.</p> <p>1<sup>st</sup> &amp; 2<sup>nd</sup> B1 for hypotheses. Accept <math>\mu_1, \mu_2</math> or <math>\mu_A, \mu_B</math> etc if it is clear which is which.<br/>1<sup>st</sup> M1 for an attempt at se with 3 out of 4 values correct.<br/>Condone switching 10 and 8: <math>\sqrt{\frac{10^2 \text{ or } 8^2}{60} + \frac{8^2 \text{ or } 10^2}{55}}</math><br/>2<sup>nd</sup> dM1 dependent on 1<sup>st</sup> M1 for a correct numerator (must have - 6) and fit their se.<br/>1<sup>st</sup> A1 for awrt 1.19<br/>3<sup>rd</sup> B1 for <math>\pm 1.6449</math> seen or probability of awrt 0.117, Sign must match their test statistic.<br/>3<sup>rd</sup> dM1 dep. on 1<sup>st</sup> M1 for a correct statement based on their normal cv and their test statistic. Ignore their hypotheses. Allow accept <math>H_0</math> but reject <math>H_1</math> is M0. Can be implied by correct conclusion.<br/>2<sup>nd</sup> A1cso for correct comment in context dependent upon all other marks being awarded.<br/><b>Must</b> mention merchandise, standard and premium ticket holders and 6 <u>or</u> manager and belief or claim<br/>NB Use of cv for difference in means <math>D</math> will have <math>D = 6 + 1.6449 \times \text{s.e.} = \text{awrt } 8.33</math> and requires sight of <math>d = 8</math> with a comment for the 3<sup>rd</sup> M1</p> <p>1<sup>st</sup> B1 for mentioning large samples <b>and</b> CLT<br/>2<sup>nd</sup> dB1 dependent on 1<sup>st</sup> B1 for stating <b>no need to</b> assume normality. Require merchandise sold not mean merchandise sold.</p> |  |

| Question Number          | Scheme   | Marks   |
|--------------------------|--|---|
| <p>3. (a)</p> <p>(b)</p> | <p><math>\bar{x} = \hat{\mu} = 1.55</math>      cao    1.55</p> <p><math>s^2 = \frac{\sum x^2 - 4 \times 1.55^2}{3} = \frac{17}{300}</math>      awrt 0.057</p> <p><math>\sum x^2 = 9.78</math>, "<math>\sum x^2</math>" &gt; 9.61, "<math>\sum x^2</math>" <math>\neq</math> <math>(\sum x)^2 = 38.44</math></p> <p>Or <math>s^2 = \frac{0.25^2 + 0.15^2 + 0.15^2 + 0.25^2}{3} = \frac{17}{300}</math></p> <p><math>P( \mu - \hat{\mu}  &lt; 0.1) = 0.99</math></p> <p><math>\frac{0.1}{\frac{0.5}{\sqrt{n}}} = 2.5758</math>      awrt 2.576</p> <p><math>n = \left(\frac{2.5758 \times 0.5}{0.1}\right)^2 (= 12.879^2 = 165.8\dots)</math></p> <p>Sample size (<math>n \geq</math>) 166</p>   | <p>B1</p> <p>M1A1ftA1</p> <p>(4)</p> <p>M1B1A1ft</p> <p>dM1A1ft</p> <p>A1 cso</p> <p>(6)</p> <p><b>Total 10</b></p> |
| <b>Notes</b>             |  |   |
| <p>(a)</p> <p>(b)</p>    | <p>1<sup>st</sup> B1 1.55 correct answer only</p> <p>1<sup>st</sup> M1 for a correct expression ft their <math>\bar{x}</math></p> <p>1<sup>st</sup> A1ft for a fully correct expression ft their <math>\bar{x}</math> only</p> <p>2<sup>nd</sup> A1 accept awrt 0.057</p> <p>1<sup>st</sup> M1 <math>\frac{0.1}{\frac{\text{their } s}{\sqrt{n}}} = z</math> value. Accept with an inequality in any direction.</p> <p>1<sup>st</sup> B1 2.5758</p> <p>1<sup>st</sup> A1ft for any equivalent form. Allow ft of <math>z = 2.326</math> or awrt 3.090. Must use 0.5</p> <p>2<sup>nd</sup> dM1 for attempt to solve for <math>n</math> dependent on 1<sup>st</sup> M leading to <math>n =</math></p> <p>2<sup>nd</sup> A1 for <math>\left(\frac{2.5758 \times 0.5}{0.1}\right)^2</math> Allow ft for 135.2... or 238.7...</p> <p>3<sup>rd</sup> A1 for 166 cao</p> |   |

| Question Number                     | Scheme  | Marks  |
|-------------------------------------|---|--|
| <p>4. (a)</p> <p>(b)</p> <p>(c)</p> | $2 \times 2.5758 \times \frac{\sigma}{\sqrt{120}} = 0.47027... \sigma$ <p><math>H_0 : \mu = 6 \quad H_1 : \mu \neq 6</math><br/>(Significance level = )10%<br/>(6 is in the interval so not significant, do not reject <math>H_0</math>) <math>\mu = 6</math></p> $1.6449 \times \frac{\sigma}{\sqrt{100}} = (6.25 - 5.14) / 2 (= 0.555)$ <p><math>\sigma = 3.374...</math></p>   | <p>M1B1A1</p> <p>(3)</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>(3)</p> <p>M1B1</p> <p>A1</p> <p>(3)</p> <p><b>Total 9</b></p> |
| <b>Notes</b>                        |   |  |
|                                     | <p>(a) 1<sup>st</sup> M1 Use of <math>2z \frac{\sigma}{\sqrt{n}}</math> with <math>z &gt; 2</math><br/>1<sup>st</sup> B1 2.58 or better<br/>1<sup>st</sup> A1 awrt <math>0.47 \sigma</math></p> <p>(b) 1<sup>st</sup> B1 Both hypotheses in terms of <math>\mu</math>.<br/>2<sup>nd</sup> B1 10%<br/>3<sup>rd</sup> B1 Correct comment leading to accepting <math>H_0</math></p> <p>(c) 1<sup>st</sup> M1 for <math>z \frac{\sigma}{\sqrt{100}} = 0.555</math> oe, using <math>n = 100</math> and where <math> z  &gt; 1.5</math><br/>1<sup>st</sup> B1 for 1.6449 or better in an attempt (could be <math>1.6449\sigma = c</math> or even <math>1.6449 \sigma^2 = c</math>)<br/>1<sup>st</sup> A1 awrt 3.37. Allow awrt 3.38 from use of <math>z = 1.64</math></p> |  |



| Question Number | Scheme   | Marks                             |
|-----------------|--|-----------------------------------|
| 5 (a)           | (Let $W = L - 3C$<br>$E(W) = 2800 - 3 \times 1000 = -200$<br>$Var(W) = 650^2 + 3^2 \times 250^2 = 985\,000$<br>$P(W > 0) = P(Z > \frac{200}{\sqrt{985000}}) = P(Z > 0.20157\dots) = 0.42015$ (calc) <u>or</u> 0.4207 (tables)  | B1<br>B1<br>M1A1<br>dM1 A1<br>(6) |
| (b)             | ( $F = C_1 + C_2 + \dots + C_8 + L_1 + L_2 + L_3$ )<br>$E(F) = 16400$<br>$Var(F) = 8 \times 250^2 + 3 \times 650^2 = 1767500$<br>$P(F > 20\,000) = P(Z > \frac{20000-16400}{\sqrt{1767500}}) = P(Z > 2.7078\dots) = 0.003386\dots$ (calc) <u>or</u> 0.0035 (tables) or 0.0034 (interpolation)  | B1<br>M1A1<br>dM1,A1<br>(5)       |
| (c)             | Assume <b>selection</b> of cars and lorries is <b>random</b> .<br><b>Weights</b> of cars and lorries are <b>independent</b> .  | B1<br>(1)                         |
| <b>Notes</b>    |  |                                   |
| (a)             | 1 <sup>st</sup> B1 for forming a suitable variable. May be implied by correct variance.<br>2 <sup>nd</sup> B1 for $-200$ cao or $200$ if their $W = 3C - L$<br>1 <sup>st</sup> M1 for attempting $Var(W) = Var(L) + 3^2 \times Var(C)$ . Condone swapping $L$ and $C$ .<br>1 <sup>st</sup> A1 for $985\,000$ cao<br>2 <sup>nd</sup> M1 dependent upon first M1 for standardising with their $-200$ and their $985000$<br>2 <sup>nd</sup> A1 awrt $0.420-0.421$ |                                   |
| (b)             | 1 <sup>st</sup> B1 for $16400$ cao<br>1 <sup>st</sup> M1 for attempting $Var(F) = 8 \times Var(C) + 3 \times Var(L)$<br>1 <sup>st</sup> A1 for $1\,767\,500$ cao<br>2 <sup>nd</sup> M1 dependent upon first M1 for standardising with their $16400$ and their $1767500$<br>2 <sup>nd</sup> A1 awrt $0.003-0.004$   |                                   |
| (c)             | Either random selection or independent weights   |                                   |
| <b>Total 12</b> |  |                                   |

| Question Number   | Scheme  | Marks             |                             |                     |                             |                     |   |    |       |       |       |   |    |      |     |    |   |    |       |      |       |   |    |      |      |       |   |    |       |       |       |  |
|---|---|-------------------|-----------------------------|---------------------|-----------------------------|---------------------|---|----|-------|-------|-------|---|----|------|-----|----|---|----|-------|------|-------|---|----|------|------|-------|---|----|-------|-------|-------|--|
| <p><b>6(a)</b></p>  | <p><math>H_0 : B(4, 0.5)</math> is a suitable model <math>H_1 : B(4, 0.5)</math> is not a suitable model</p> <table border="1" data-bbox="284 264 1042 517"> <thead> <tr> <th>Even number count</th> <th><math>O_i</math></th> <th><math>E_i</math></th> <th><math>\frac{(O_i - E_i)^2}{E_i}</math></th> <th><math>\frac{O_i^2}{E_i}</math></th> </tr> </thead> <tbody> <tr> <td>0</td> <td>12</td> <td>9.375</td> <td>0.735</td> <td>15.36</td> </tr> <tr> <td>1</td> <td>45</td> <td>37.5</td> <td>1.5</td> <td>54</td> </tr> <tr> <td>2</td> <td>36</td> <td>56.25</td> <td>7.29</td> <td>23.04</td> </tr> <tr> <td>3</td> <td>39</td> <td>37.5</td> <td>0.06</td> <td>40.56</td> </tr> <tr> <td>4</td> <td>18</td> <td>9.375</td> <td>7.935</td> <td>34.56</td> </tr> </tbody> </table> <p><math>E_i = 150 \times P(X = i)</math></p> <p><math>\chi^2 = \sum \frac{(O_i - E_i)^2}{E_i}</math> or <math>\chi^2 = \sum \frac{O_i^2}{E_i} - N</math></p> <p><math>\chi^2 = 17.52</math> or <math>\chi = 167.52 - 150 = 17.52</math> awrt 17.5</p> <p><math>\nu = 4, \chi_4^2(1\%) = 13.277</math></p> <p>(Reject <math>H_0</math>.) <math>B(4, 0.5)</math> is not a suitable model or David's claim incorrect.</p> <p><b>(b)</b> <math>\hat{p} = \frac{0 \times 12 + 1 \times 45 + 2 \times 36 + 3 \times 39 + 4 \times 18}{4 \times 150} = 0.51</math></p> <p><b>(c)</b> <math>d = 150 \times 6 \times 0.51^2 \times 0.49^2 = 56.205009</math> awrt 56.2<br/> <math>e = 150 - (8.65 + 36.00 + 39.00 + "d") = 10.144991</math> awrt 10.1 or 10.2<br/> or <math>e = 150 \times 0.51^4 = 10.1478015</math></p> <p><b>(d)</b> <math>H_0 : B(4, p)</math> is a suitable model <math>H_1 : B(4, p)</math> is not a suitable model</p> <p><b>(e)</b> <math>\nu = 3, \chi_3^2(1\%) = 11.345</math><br/> <math>(16.9 &gt; 11.345)</math> Reject <math>H_0</math><br/> Binomial is not a suitable model or John's claim incorrect or equivalent contextualised statement that rejects the Binomial model.</p> | Even number count | $O_i$                       | $E_i$               | $\frac{(O_i - E_i)^2}{E_i}$ | $\frac{O_i^2}{E_i}$ | 0 | 12 | 9.375 | 0.735 | 15.36 | 1 | 45 | 37.5 | 1.5 | 54 | 2 | 36 | 56.25 | 7.29 | 23.04 | 3 | 39 | 37.5 | 0.06 | 40.56 | 4 | 18 | 9.375 | 7.935 | 34.56 | <p>B1</p> <p>M1A1</p> <p>M1A1</p> <p>A1</p> <p>B1, B1ft</p> <p>A1</p> <p>(9)</p> <p>M1 A1</p> <p>(2)</p> <p>M1, A1</p> <p>B1ft</p> <p>(3)</p> <p>B1</p> <p>(1)</p> <p>B1B1ft</p> <p>B1</p> <p>(3)</p> <p><b>Total 18</b></p> |
| Even number count   | $O_i$   | $E_i$             | $\frac{(O_i - E_i)^2}{E_i}$ | $\frac{O_i^2}{E_i}$ |                             |                     |   |    |       |       |       |   |    |      |     |    |   |    |       |      |       |   |    |      |      |       |   |    |       |       |       |  |
| 0   | 12  | 9.375             | 0.735                       | 15.36               |                             |                     |   |    |       |       |       |   |    |      |     |    |   |    |       |      |       |   |    |      |      |       |   |    |       |       |       |  |
| 1   | 45  | 37.5              | 1.5                         | 54                  |                             |                     |   |    |       |       |       |   |    |      |     |    |   |    |       |      |       |   |    |      |      |       |   |    |       |       |       |  |
| 2   | 36  | 56.25             | 7.29                        | 23.04               |                             |                     |   |    |       |       |       |   |    |      |     |    |   |    |       |      |       |   |    |      |      |       |   |    |       |       |       |  |
| 3   | 39  | 37.5              | 0.06                        | 40.56               |                             |                     |   |    |       |       |       |   |    |      |     |    |   |    |       |      |       |   |    |      |      |       |   |    |       |       |       |  |
| 4   | 18  | 9.375             | 7.935                       | 34.56               |                             |                     |   |    |       |       |       |   |    |      |     |    |   |    |       |      |       |   |    |      |      |       |   |    |       |       |       |  |
| <b>Notes</b>  |   |                   |                             |                     |                             |                     |   |    |       |       |       |   |    |      |     |    |   |    |       |      |       |   |    |      |      |       |   |    |       |       |       |  |
| <p><b>(a)</b></p> <p><b>(b)</b></p> <p><b>(c)</b></p> <p><b>(d)</b></p> <p><b>(e)</b></p> | <p>1<sup>st</sup> B1 Accept 'Binomial with <math>p = 0.5</math>' replacing 'B(4, 0.5)'</p> <p>1<sup>st</sup> M1 for attempt at <math>E_i = 150 \times P(X = i)</math> with at least 2 values correct.</p> <p>1<sup>st</sup> A1 at least 4 <math>E_i</math> correct to 3sf cao. Condone truncation.</p> <p>2<sup>nd</sup> M1 for at least 2 correct calculations from 4<sup>th</sup> or 5<sup>th</sup> column.</p> <p>2<sup>nd</sup> A1 at least 4 correct to 3sf from 4<sup>th</sup> or 5<sup>th</sup> column. Condone truncation.</p> <p>3<sup>rd</sup> A1 for a test statistic of awrt 17.5 Answer only implies 2ndM1 2ndA1 3rdA1</p> <p>4<sup>th</sup> A1 for correct conclusion rejecting binomial model. Condone missing parameters here.</p> <p>Award provided their test statistic <math>&gt; 11.345</math></p> <p>1<sup>st</sup> M1 for attempting <math>\hat{p} = \frac{\sum Ex}{600}</math> with at least 2 values on the numerator correct</p> <p>1<sup>st</sup> A1 for 0.51 cao</p> <p>1<sup>st</sup> M1 <math>d = 150 \times 6 \times (\text{their } \hat{p})^2 \times (1 - \text{their } \hat{p})^2</math></p> <p>1<sup>st</sup> A1 awrt 56.2</p> <p>1<sup>st</sup> B1ft awrt 10.1 or follow from "d"</p> <p>1<sup>st</sup> B1 accept <math>H_0</math>: Binomial is a suitable model <math>H_1</math>: Binomial is not a suitable model</p> <p>1<sup>st</sup> B1 <math>\nu = 3</math>, 2<sup>nd</sup> B1 11.345, follow through their <math>\nu \neq</math> their value in part (a)</p> <p>3<sup>rd</sup> B1 Correct statement rejecting <math>H_0</math></p>   |                   |                             |                     |                             |                     |   |    |       |       |       |   |    |      |     |    |   |    |       |      |       |   |    |      |      |       |   |    |       |       |       |  |

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